

# CS305: Homework 1

---

**Assigned:** Saturday, September 24, 2022

**Due:** Monday, October 3, 2022

- Do all of the following problems. **Show your work.** Homework submissions must be emailed to me **as a pdf.**
- You may work with others on the homework, but you **MUST** acknowledge the people you worked with at the top of your homework submission. Do **not** look at the web for solutions to homework problems. Looking for solutions does **not** help your problem solving powers.

## Problems

Note that the book separates things into exercises and problems with exercises appearing at the end of a section and problems (which tend to be longer) appearing at the end of the chapter.

1. For each, either prove it is true (by using the definition of  $O$  and  $\Omega$ ) or state that it isn't true
  - (a)  $2n^3 + 4n$  is  $O(n^5)$
  - (b)  $2n^3 + 4n$  is  $\Omega(n^3)$
  - (c)  $2n^3 + 4n$  is  $O(n^3)$
2. Answer these with (Yes or No) or (True or False) and a sentence why.
  - (a) Is  $2n^3 - 4n \in \Theta(n^3)$ ?
  - (b) Can you say that  $n^3$  is an asymptotically tight bound for  $2n^3 - 4n$ ?
  - (c) Is  $n^2$  an asymptotic lower bound for  $2n^3 - 4n$ ?
  - (d)  $n^2$  is  $o(n^4)$  Note: little o, not big O
  - (e)  $n^2$  is  $o(n^3)$
  - (f)  $n^2$  is  $o(n^2)$
  - (g)  $n^2$  is  $o(n)$
  - (h)  $8^{lg n}$  is  $\Theta(n^3)$

---

3. Suppose algorithm A runs in  $\Theta(n)$  time and algorithm B runs in  $\Theta(n \lg n)$  time. Answer True or False for each and give a one sentence reason.

- (a) There may be values of  $n$  for which algorithm A runs faster than algorithm B.
- (b) There may be values of  $n$  for which algorithm B runs faster than algorithm A.
- (c) There is some value of  $n$ , such that for all values of  $n$  larger than that value, algorithm A runs faster than algorithm B.
- (d) There is some value of  $n$ , such that for all values of  $n$  larger than that value, algorithm B runs faster than algorithm A.
- (e) There may be a value for  $n$  for which algorithms A and B take the same amount of time.

4. In the 4th edition of textbook, Problem 4-2 Parameter Passing Costs

5. Determine asymptotically tight bounds for each of the following by the Master Theorem (see p. 94) if possible (and show why the appropriate case holds). If not possible by the Master Theorem, just indicate why.

(a)  $T(n) = 8T(n/2) + 5n^3 + n^2$

(b)  $T(n) = 7T(n/2) + n^3$