

CS 230
Programming Languages

12 / 01 / 2022

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Today's Topics

- Questions? / Comments?
- Chapter 11 & 12 --- Abstract Data Types / Encapsulation / Object Oriented Programming Language features
- Chapter 16 – Logic Programming Languages

Anyone know the key features
required of a language to be
considered Object-Oriented?

Abstraction/Encapsulation/OOP

- Chapters 11 & 12
 - Abstraction
 - Information Hiding
 - Object Oriented Programming Language features

Chapter 11 & 12

- Abstraction
 - Process abstraction
 - Making a method/function/subprogram to handle some task
 - Data abstraction
 - Records (data only) OR abstract data types (data and member methods)
 - Example: floating point

Chapter 11 & 12

- Information hiding
 - is a key concept of data abstraction
- User defined ADTs
 - representation of the type is hidden from rest of program that uses them = Information Hiding
 - declarations of the type and ops/methods contained in a single unit = Encapsulation
 - e.g. a class
 - one can then create variables of these types

Chapter 11 & 12

- Parameterized ADTs
 - the ability to create a class that can hold data of any appropriate type (to be specified when used)
 - e.g. create a stack class that can hold any kind of data (e.g. stack of ints, stack of strings, etc.)
 - In C++ this is handled via templates
 - In Java
 - Pre 5.0 – used Object as the type (need to cast to actual type to use)
 - Starting in 5.0 – uses generics (type specified in angle brackets, no casting needed), better design

Chapter 11 & 12

- Benefits of information hiding
 - Reliability
 - reduction of what the programmer needs to be aware of can change the implementation
 - (e.g. stack may have been implemented as a linked list but then say you need to change it due to memory problems --- can use a contiguous data structure, an array) and the clients of the stack do NOT need to update any of their code ...

Chapter 11 & 12

- A language that is an OOPL must contain support for
 - ADTs
 - Inheritance
 - Dynamic binding of method calls to methods

Chapter 11 & 12

- Inheritance
 - What do we know about inheritance?
- Dynamic binding of method calls to methods
 - What do we know about dynamic method binding?

Logic Languages

- Logic (or Declarative) languages
 - Express programs in a form of symbolic logic
 - Produce results via logical inferences
- Logic programs
 - specify the desired results
 - instead of creating the procedures (or functions) to produce them
- Since we are writing no procedures, the syntax of logic languages is quite different from imperative (e.g. C, C++, Java) or even Functional (e.g. LISP, Scheme)

Logic Languages

- Logic languages are based on formal logic
- Prolog is a Logic Programming Language
- Prolog was developed by people with interests in
 - Natural language processing
 - Automated theorem proving

Logic Languages

- Symbolic logic can be used for the basic needs of formal logic:
 - express propositions (defined on next slide)
 - express relationships between propositions
 - describe how new propositions can be inferred from other propositions
- Particular form of symbolic logic used for logic programming called predicate calculus

Logic Languages

- Some terminology
- Proposition --- logical stmt that may or may not be true
 - Represented by simple terms.
 - Terms are either constants or variables
 - A constant represents an object
 - A variable can represent different objects at different times
- An atomic proposition consists of compound terms
 - Compound term – one element of a mathematical relation --- looks like mathematical function notation with names and parentheses.
 - Two parts are:
 - Functor
 - Ordered list of parameters

Logic Languages

- Compound term
 - The compound terms are also called tuples. 1-tuples, 2-tuples, 3-tuples, 4-tuples ...
 - Depending on the number of parameters

- Compound term examples:

student(jon)

like(seth, OSX)

like(nick, windows)

like(jim, linux)

- The meaning of the relations (i.e. student and like) are up to the programmer.

Logic Languages

- The meaning of the relations are up to the programmer.
- For instance
 - `like(jim, linux)`
 - Could mean jim likes linux. Or it could mean jim is similar to linux. Or it could mean something else entirely.
- There is no intrinsic semantics.
- If the relations are named well though, the programs obviously become more readable.

Logical connectors

Name	Symbol	Example	Meaning
negation	\neg	$\neg a$	not a
conjunction	\cap	$a \cap b$	a and b
disjunction	\cup	$a \cup b$	a or b
equivalence	\equiv	$a \equiv b$	a is equivalent to b
implication	\supset	$a \supset b$	a implies b
	\subset	$a \subset b$	b implies a

Logic Languages

- Logical operators
 - Conjunction (and) is like intersection among sets.
 - Disjunction (or) is like union among sets.
- Implication
 - a implies b can be read as "if a , then b "

Logic Languages

- Precedence:
 - Negation
 - Conjunction, Disjunction, Equivalence
 - Implication

Logic Languages

- So far we've seen only constants in these propositions, e.g. jim, linux, etc.
- To use a variable in a proposition we need to preface it with either “for all” or “there exists”
- These are quantifiers
 - For all is represented by an upside-down A
 - There exists is represented by a backwards E
- Predicate calculus consists of the logical connectors we just saw in addition to the two quantifiers above.

Logic Languages

- For Predicate Calculus, (that is using the logical connectors and the quantifiers) it should be obvious that there are many ways to state the same thing
- Anyone want to give an example?

Logic Languages

- For Predicate Calculus, (that is using the logical connectors and the quantifiers) it should be obvious that there are many ways to state the same thing
- Anyone want to give an example?
 - Any of DeMorgan's laws
 - e.g. $\text{not } (a \text{ and } b) = (\text{not } a) \text{ or } (\text{not } b)$
 - Let me write up the truth table showing this equivalence

Logic Languages

- Because there are many ways to state the same thing, a standard form for propositions was decided

- Clausal form:

$$B_1 \cup B_2 \cup \dots \cup B_n \subset A_1 \cap A_2 \cap \dots \cap A_m$$

means if all the A s are true, then at least one B is true

- Antecedent: right side

- Consequent: left side

Logic Languages

- The A's and B's in the clausal form can be variables or constants.
- When they are variables, the “for all” quantifier is implied.
- Note: the meaning of variable here is different than the meaning we associate with variables in imperative languages.
- Clausal form can be used exclusively because:
 - All predicate calculus propositions can be algorithmically converted to clausal form. So, we do not lose generality by restriction to this form of propositions.

Logic Languages

- Some examples:

$C \subset A \cap B$

ForAll X .($\text{mammal}(X) \subset \text{dog}(X)$)

ThereExists X .($\text{father}(\text{bob}, X) \cap \text{female}(X)$)

- Taken separately, read each of the above in English.

Logic Languages

- Some examples:

$$C \subset A \cap B$$

if both A and B are true, then C is true.

ForAll X.(mammal(X) \subset dog(X))

All dogs are mammals

ThereExists X.(father(bob,X) \cap female(X))

bob has a daughter

Predicate Calc and proving theorems

- One use of propositions is to discover new theorems that can be inferred from known theorems
- Resolution: an inference principle that allows inferred propositions to be computed from given propositions
- A simple example:

$\text{older}(\text{joanne}, \text{jake}) \subset \text{mother}(\text{joanne}, \text{jake})$

$\text{wiser}(\text{joanne}, \text{jake}) \subset \text{older}(\text{joanne}, \text{jake})$

New propositions can be inferred from resolution:

$\text{wiser}(\text{joanne}, \text{jake}) \subset \text{mother}(\text{joanne}, \text{jake})$

Predicate Calc and proving theorems

- The presence of variables in propositions requires resolution to find values for those variables that allow the matching process to succeed. This is called unification.
- Instantiation is the temporary assigning of values to variables.
- During some resolutions, instantiating some temporary values might cause the matching process to fail, at which time, backtracking must occur to instantiate a different value to the variable.

Predicate Calc and proving theorems

- One possible way to prove a theorem is by contradiction.
- Make a proposition that is the theorem negated.
- The theorem is then attempted to be proved by finding an inconsistency.

- This is a theoretically useful way to prove theorems, but in practice the time it takes might be too long.
- Theorem proving is the basis for logic programming so we need a faster way for it to be able to do it.

Predicate Calc and proving theorems

- A restricted kind of clausal form is used when propositions are used for resolution. These special kinds of propositions are **Horn clauses**
 - Only 2 forms
 - A single atomic proposition on left side
 - Or
 - Empty left side
- Left side is called the *head*. If left side is not empty the Horn clause is called a *headed Horn clause*.
- Anyone recall what an atomic proposition is?

Predicate Calc and proving theorems

- An atomic proposition is a functor and a set of parameters in parentheses.
 - e.g. $\text{mother}(\text{joanne}, \text{jake})$
- A headed Horn clause example:
 - $\text{older}(\text{joanne}, \text{jake}) \subset \text{mother}(\text{joanne}, \text{jake})$
 - these state relationships among relations
- What do you think the purpose of headless Horn clauses might be? e.g. $\text{mother}(\text{joanne}, \text{jake})$
- Not all propositions can be stated as/converted to Horn clauses, so there is a loss of generality.

Overview of Logic Programming

- Logical programming is nonprocedural
 - Programs do not state how a result is to be computed, but rather the form of the result
- We don't tell the computer how to get a result. Instead we state the form of the result and let the logic programming “engine” determine how to get that result.
- We provide the relevant information via the predicate calculus and the computer infers the results using resolution.

Overview of Logic Programming

- Describe the characteristics of a sorted list, not the process of rearranging a list

$\text{sort}(\text{old_list}, \text{new_list}) \subset$
 $\text{permute}(\text{old_list}, \text{new_list}) \cap \text{sorted}(\text{new_list})$

$\text{sorted}(\text{list}) \subset \text{ForAll } j \text{ such that } 1 \leq j < n, \text{list}(j) \leq \text{list}(j+1)$

- This says that if a list is in non-decreasing order, it is sorted. Also, if the `old_list` is a permutation of the `new_list` and the `new_list` is sorted, then that's what it means to sort an `old_list` to be the `new_list`

Prolog

- Our text uses the Edinburgh Syntax version of Prolog
- **Term**: a constant, variable, or structure
- **Constant**: an atom or an integer
- **Atom**: symbolic value of Prolog
- Atom consists of either:
 - a string of letters, digits, and underscores beginning with a lowercase letter
 - a string of printable ASCII characters delimited by apostrophes

Prolog

- **Variable**: any string of letters, digits, and underscores beginning with an uppercase letter
- **Instantiation**: binding of a variable to a value
 - Lasts only as long as it takes to satisfy one complete goal
- **Structure**: represents atomic proposition
functor(parameter list)

Prolog

- Fact statements
 - Headless Horn clauses

student (jonathan) .
brother (tyler, cj) .
- Rule statements
 - Headed Horn clauses
 - Right side: **antecedent** (*if* part)
 - May be single term or conjunction
 - Left side: **consequent** (*then* part)
 - Must be single term
- **Conjunction**: multiple terms separated by logical AND operations (implied)

Prolog

```
parent(kim,kathy) :- mother(kim,kathy) .
```

- Can use variables (universal objects) to generalize meaning:

```
parent(X,Y) :- mother(X,Y) .
```

```
sibling(X,Y) :- mother(M,X) ,
```

```
    mother(M,Y) ,
```

```
    father(F,X) ,
```

```
    father(F,Y) .
```

Prolog

- GOAL STATEMENTS
- For theorem proving, a theorem is in the form of a proposition that we want the system to prove or disprove
- Same format as headless Horn

student (james)

- this asks if james is a student, it either fails (james is not a student) or it doesn't (james is indeed a student)
- Conjunctive propositions and propositions with variables are also legal goals

father (X, joe)

- this asks for all fathers of joe, if any, otherwise it fails.

Prolog

- INFERRNCING
- Queries are called goals
- If a goal is a compound proposition, each of the facts is a subgoal
- To prove a goal is true, the system must find a chain of inference rules and/or facts. For goal Q:

B :- A

C :- B

...

Q :- P

- Process of proving a subgoal is called **matching, satisfying, or resolution**

Prolog

- POSSIBLE WAYS TO INFER
- Bottom-up resolution, forward chaining
 - Begin with facts and rules of database and attempt to find sequence that leads to goal
- Top-down resolution, backward chaining
 - begin with goal and attempt to find sequence that leads to set of facts in database
- Prolog implementations use **backward chaining**

Prolog

- POSSIBLE WAYS TO INFER
- When goal has more than one subgoal, can use either
 - *Depth-first search*: find a complete proof for the first subgoal before working on others
 - *Breadth-first search*: work on all subgoals in parallel
- Prolog uses **depth-first search**
 - Can be done with fewer resources so it is preferred for use in Prolog

Prolog

- Backtrack during inference
- For a goal with multiple subgoals, if fail to show truth of one of subgoals, reconsider previous subgoal to find an alternative solution: **backtracking**
- Begin search where previous search left off
- In worst case, can take lots of time and space because may find all possible proofs to every subgoal

Prolog

- Recap: When trying to prove a goal, Prolog uses
 - backward chaining (starting at goal) to try to find facts that satisfy it
 - depth first search when satisfying a chain of subgoals
 - backtracking during inference to possibly get an alternative solution to an earlier subgoal

Prolog

- Prolog also supports integer variables and integer arithmetic
- *is* operator: takes an arithmetic expression as right operand and variable as left operand
- $A \text{ is } B / 10 + C$
- Not the same as an assignment statement
- B & C must have been instantiated and A must not have been instantiated for that expression to have A take on the value of the expression.
- But if A is instantiated prior to this expression or B or C are not instantiated, then the clause is not satisfied and no instantiation can take place.
- Example: $\text{Sum is Sum} + \text{Number}$. Is this possible?

Prolog

```
speed(ford,100) .  
speed(chevy,105) .  
speed(dodge,95) .  
time(ford,20) .  
time(chevy,21) .  
time(dodge,24) .  
distance(X,Y) :- speed(X,Speed) ,  
                  time(X,Time) ,  
                  Y is Speed * Time.
```

- Here, the facts are the first six statements and the last is a rule stating the relationship between time, speed and distance.
- Example query: `distance(chevy, Chevy_Distance)`
- `Chevy_Distance` is instantiated with the value 2205

Prolog

- TRACE
- Tracing model of execution - four events:
 - Call (beginning of attempt to satisfy goal)
 - Exit (when a goal has been satisfied)
 - Redo (when backtrack occurs)
 - Fail (when goal fails)

Prolog

`likes (jake, chocolate) .`
`likes (jake, apricots) .`
`likes (darcie, licorice) .`
`likes (darcie, apricots) .`

`trace.`

`likes (jake, X) ,`
`likes (darcie, X) .`

This is asking, what is X such that
both jake and darcie like X

Let's trace it on the board.

